

Measurement of optical path length change following pulsed laser irradiation using differential phase optical coherence tomography

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Abstract. Differential phase optical coherence tomography (DPOCT) is introduced to measure optical path length changes in response to pulsed laser irradiation (585 nm). An analytical equation that includes thermoelastic surface displacement and thermorefractive index change is derived to predict optical path length change in response to pulsed laser irradiation for both “confined surface” and “free surface” model systems. The derived equation is tested by comparing predicted values with data recorded from experiments using two model systems. Thermorefractive index change and the thermal expansion coefficient are deduced from differential phase change ($d\Delta\phi$) and temperature increase (ΔT_0) measurements. The measured $n(T_0)\beta(T_0) + dn/dT = 1.74 \cdot 10^{-4} \pm 1.7 \cdot 10^{-6}$ (1/K) in the free surface experiment matches with the National Institute of Standards and Technology (NIST) data value [$= 1.77 \cdot 10^{-4}$ (1/K)]. Exclusion of lateral thermal expansion in the analytical model for the confined surface experiment causes difference between the measured dn/dT [$= -2.3 \cdot 10^{-4} \pm 7.3 \cdot 10^{-6}$ (1/K)] and the NIST value [$= -9.45 \cdot 10^{-5}$ (1/K)]. In spite of the difference in the confined surface experiment, results of our studies indicate DPOCT can detect dynamic optical path length change in response to pulsed laser irradiation with high sensitivity, and applications to tissue diagnostics may be possible. © 2006 Society of Photo-Optical Instrumentation Engineers. [DOI: 10.1117/1.2236289]

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1 Introduction

Photothermal (PT) response is generated by the heating of a sample due to absorption of electromagnetic radiation in a short pulse or continuous train of pulses.¹ Absorption of pulsed laser radiation in a sample generates PT effects, including a temperature increase, refractive index change, and thermoelastic surface displacement.¹ Detection of PT effects and associated signal processing have been applied in many areas including photoacoustic spectroscopy, nondestructive evaluation, and thermal property determination.²

The detection of laser-induced optical path length change as a photothermal effect may aid tissue diagnostics in biomedical applications such as imaging³ and sensing.⁴ Optical path length changes in tissue in response to absorption of pulsed laser light result from refractive index change.⁵ Thermal expansion as well as refractive index change results in a transient optical path length variation in laser-heated tissue.⁵ Spatial variation of refractive index is a fundamental optical

property of tissue and can provide useful and critical information about structure and physiological function.

Because water and protein are primary constituents of all living systems, relevant optical and thermal properties are of interest in investigating optical effects in tissue. Fortunately, national and international standards organizations have invested substantial resources in characterizing the thermo-physical properties of water. For proteins, substantially less data are available relating to refractive index and variation with temperature and pressure. The dependence of water refractive index on temperature has been measured⁶⁻⁸ and a formulation for the refractive index of water in the temperature range of -10 to 500°C was published over the wavelength range of 0.2 to $2.5 \mu\text{m}$.⁸ The formulation was based on data collected by Thormählen, Straub, and Grigull.⁹ Most published data relate to refractive index of water in the visible wavelength range. Direct measurement of water refractive index in the near infrared (NIR) is complicated by thermal effects induced by absorption of the probing radiation.⁶ For refractive index change in the IR, studies using interferometers, including Fabry-Perot and Mach-Zehnder configurations,

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have produced the most accurate data.⁷ Richerzhagen used a single Michelson interferometer to measure refractive index of liquid water. In these experiments, water in a thermally isolated cell is maintained at a constant temperature by external circulation, which allows direct refractive index measurement without knowledge of thermal expansion.⁷ Water refractive index was measured by displacing a mirror positioned inside the water cell.⁷ For thermal expansion measurement, Takenaka and Masui measured thermal expansion of pure water by the dilatometric method in a temperature range from 0 to 85 °C.¹⁰ However, the dilatometer requires a mercury bulb that is connected to the water cell covered by a thermostat. Therefore, a noninvasive optical interferometric technique to measure both refractive index change and thermal expansion with higher sensitivity may be useful.

Optical coherence tomography (OCT) was introduced as a technique to record a cross sectional image of subsurface tissue structure with micron-scale resolution.¹¹ Conventional OCT has been used as a promising diagnostic modality for imaging a variety of tissues and detecting tissue structures.^{12,13} However, photothermal response requires a relative strain or stress change measurement related to light absorption by specific tissue chromophores. Correspondingly, detection of laser-induced thermoelastic displacement requires measurement of relative displacement between two points in a sample to deduce optical path length change due to thermal expansion.¹⁴

Differential phase optical coherence tomography (DPOCT) is introduced in this study to measure the optical path length changes resulting from absorption of pulsed laser radiation. DPOCT is a birefringent-fiber-based dual-channel low-coherence Michelson interferometer that is capable of differential phase measurement between light backscattered from two spatially separated sites in a sample.¹⁵ Advantages of DPOCT are phase sensitivity as low as 10^{-3} radians¹⁶ and a high signal-to-noise ratio (SNR) due to common phase noise rejection.¹⁵ Tissue response to thermal, electrical, or chemical stimuli have been detected by DPOCT. Electrokinetic response of cartilage^{3,17} has been measured and the optical path length change due to chemical concentration change was studied for various analytes.⁴ DPOCT is capable of measuring relative phase change with laser irradiation to detect laser-induced optical path length change. The tissue response of the atherosclerotic artery³ and a human hair in an epoxy phantom¹⁴ in response to laser irradiation has been investigated. Despite these studies, a quantitative investigation of optical path length change and the relative mechanisms using DPOCT has not been completed. In this study, quantitative laser-induced optical path length change is investigated by accounting for variation induced by refractive index change and thermal expansion.

2 Materials and Methods

2.1 Theory

Optical path length (δ) in a sample is the spatial integral of the refractive index with respect to position along a path perpendicular to the wavefront. Before laser irradiation, the refractive index of a sample without external mechanical or thermal stress is assumed to be homogeneous, and optical

path length (δ) can be written as a product of refractive index and sample thickness under isothermal conditions.⁵

$$\delta(T) = \int_{z_1(T)}^{z_2(T)} n(T) dz = n(T_0) \times [z_2(T_0) - z_1(T_0)], \quad (1)$$

where $n(T_0)$ is a sample refractive index at initial temperature (T_0), and $z_1(T_0)$ and $z_2(T_0)$ are front and back surface locations in the sample, respectively.

When laser radiation is absorbed in a translucent sample, the temperature profile in the sample can be approximated by the Beer-Lambert law.

$$\Delta T(z) = \Delta T_0 \exp(-\mu_a z), \quad (2)$$

where μ_a is the absorption coefficient of the material at the laser wavelength.

In the following, an analytical model is developed that requires several assumptions

1. Constant values of thermal expansion coefficient (β) and refractive index (n) are assumed as in a homogeneous material.

2. The sample temperature distribution before laser heating is isothermal ($T=T_0$).

3. Laser pulse duration (τ_p) is shorter than thermal diffusion time according to the thermal confinement condition.¹⁸

As temperature increases, the refractive index and thermal expansion coefficient of water change linearly over the temperature range of interest ($=293-303$ K).^{6,10}

$$n(T) = n(T_0) + \frac{dn}{dT} \Delta T(z), \quad \beta(T) = \beta(T_0) + \frac{d\beta}{dT} \Delta T(z). \quad (3)$$

Thermoelastic surface deformation results from internal acoustic stress induced by laser heating. Sample deformation is given by a thermoelastic wave equation¹⁹⁻²¹

$$\begin{aligned} \rho \frac{\partial^2 u}{\partial t^2} - \frac{E}{2(1+\nu)} \nabla^2 u - \frac{E}{2(1+\nu)(1-2\nu)} \nabla (\nabla \cdot u) \\ = \frac{-E\beta}{3(1-2\nu)} \nabla (\Delta T), \end{aligned} \quad (4)$$

where u is displacement, E is a Young's modulus, ν is Poisson's ratio ($=0.5$ for water), and β is the thermal expansion coefficient.

A quasi-steady-state equilibrium occurs after the transient acoustic stress has passed, and remains until thermal diffusion occurs.¹⁹ Therefore, the first term in the thermoelastic wave equation can be ignored. Additionally, displacement only in depth (z) is taken into consideration, assuming the sample is homogeneous and the radial thermal gradient is small,²⁰ consistent with assumption 3.

$$\begin{aligned} - \frac{E}{2(1+\nu)} \frac{\partial^2 u_z}{\partial z^2} - \frac{E}{2(1+\nu)(1-2\nu)} \frac{\partial}{\partial z} \left(\frac{\partial u_z}{\partial z} \right) \\ = \frac{-E\beta}{3(1-2\nu)} \frac{\partial}{\partial z} (\Delta T). \end{aligned} \quad (5)$$

Integrating each side of the equation with respect to depth (z), the thermoelastic displacement (u_z) within the heated sample is

$$u_z = \frac{\beta(1+\nu)}{3(1-\nu)} \int_{z_1}^{z_2} \Delta T dz. \quad (6)$$

Laser-induced optical path length change (δ), including the thermorefractive (dn/dT) and the thermoelastic contributions [$n(T_0) \cdot \beta(T_0)$], are:

$$\delta(T) = \int_{z_1(T)}^{z_2(T)} n(T, z) dz = \int_{z_{s1}(T_0) + \Delta z_{s1}(T_0)}^{z_{s2}(T_0) + \Delta z_{s2}(T_0)} n(T, z) dz, \quad (7)$$

$$\begin{aligned} \delta(T) = & \int_{z_{s1}(T_0)}^{z_{s2}(T_0)} \left[n(T_0) + \frac{dn}{dT} \Delta T(z) \right] dz \\ & + \int_{z_{s1}(T_0)}^{z_{s2}(T_0)} \frac{(1+\nu)}{3(1-\nu)} \cdot \left[n(T_0) + \frac{dn}{dT} \Delta T(z) \right] \cdot \left[\beta(T_0) \right. \\ & \left. + \frac{d\beta}{dT} \Delta T(z) \right] \cdot \Delta T(z) dz, \end{aligned} \quad (8)$$

where $\Delta z_{s1}(T_0)$ and $\Delta z_{s2}(T_0)$ are displacement of the front and back surface locations in response to laser irradiation.

The first integral represents the thermorefractive contribution, while the second integral represents optical path length change by thermal expansion. When temperature increase (ΔT) in the sample is given by the Beer-Lambert law, an analytical expression for the laser-induced optical path length change may be written,

$$\begin{aligned} \delta(T) = & \{n(T_0)[z_{s2}(T_0) - z_{s1}(T_0)] \\ & + \left[n(T_0) \frac{1+\nu}{3(1-\nu)} \beta(T_0) \right. \\ & \left. + \frac{dn}{dT} \frac{\exp[-\mu_a z_{s2}(T_0)] - \exp[-\mu_a z_{s1}(T_0)]}{-\mu_a} \Delta T_0 \right. \\ & \left. + \left[n(T_0) \frac{d\beta}{dT} + \frac{dn}{dT} \beta(T_0) \right] \right. \\ & \left. \times \frac{1+\nu}{3(1-\nu)} \frac{\exp[-2\mu_a z_{s2}(T_0)] - \exp[-2\mu_a z_{s1}(T_0)]}{-2\mu_a} \Delta T_0^2 \right. \\ & \left. + \frac{dn}{dT} \frac{1+\nu}{3(1-\nu)} \frac{d\beta}{dT} \frac{\exp[-3\mu_a z_{s2}(T_0)] - \exp[-3\mu_a z_{s1}(T_0)]}{-3\mu_a} \Delta T_0^3 \right. \\ & \left. = C_0 + C_1 \cdot \Delta T_0 + C_2 \cdot \Delta T_0^2 + C_3 \cdot \Delta T_0^3, \right. \end{aligned} \quad (9)$$

where C_0, C_1, C_2 , and C_3 are constant, linear, quadratic, and cubic temperature dependence terms in optical path length change due to laser heating and are given explicitly in Eq. (9).

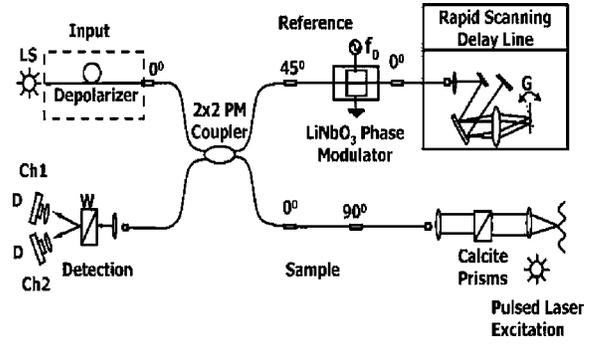


Fig. 1 Differential phase sensitive optical coherence tomography (DPOCT) system with a flashlamp pumped excitation laser (LS), lens (L), rapid scanning optical delay (RSOD) line, grating (G), detector (D), Wollaston prisms (W), and sample (S).

2.2 Differential Phase Optical Coherence Tomography System

The differential phase optical coherence tomography (DPOCT) system used in this study (Fig. 1) is a polarization maintaining (PM) fiber-based Michelson interferometer and has been previously described.^{3,4,14-17,20} DPOCT is capable of measuring an optical path length difference between backscattered light from two spatially separated sites in a sample.

Partially polarized light in a single spatial mode is emitted from an optical semiconductor amplifier [AFC Technologies Inc., Hull, Quebec, Canada, $\lambda_o = 1.31 \mu\text{m}$ and full width at half maximum (FWHM) of $\Delta\lambda = 60 \text{ nm}$] and delivered into the DPOCT system through a polarization-maintaining (PM) fiber.¹⁵ The partially polarized incident light is depolarized and decorrelated into two independent linearly polarized modes by the PM fiber.¹⁶ A lithium niobate (LiNbO_3) electro-optic waveguide phase modulator projects out components of the two depolarized modes along a single axis. The rapid scanning optical delay (RSOD) line²² compensates material and waveguide dispersion introduced by the LiNbO_3 phase modulator. Interference is formed in a 2×2 PM coupler when optical path lengths of backscattered light from reference and sample arms are equal.¹⁶ Detected light intensity in horizontal (H) and vertical (V) channels formed by interference between the sample (s) and reference (r) paths are given by,

$$I_H(\tau_H) = \langle |E_{r,H}(t)|^2 \rangle + \langle |E_{s,H}(t - \tau_H)|^2 \rangle + 2 \text{Re} \langle E_{r,H}(t) E_{s,H}^*(t - \tau_H) \rangle, \quad (10)$$

$$I_V(\tau_V) = \langle |E_{r,V}(t)|^2 \rangle + \langle |E_{s,V}(t - \tau_V)|^2 \rangle + 2 \text{Re} \langle E_{r,V}(t) E_{s,V}^*(t - \tau_V) \rangle, \quad (11)$$

where E in the first and second terms are electric field amplitudes from the reference (r) and sample (s), and τ is the relative time delay. Here, $\tau_{H,V}$ are the time delays introduced in horizontal and vertical channels by a birefringent calcite prism pair in the sample arm of the DPOCT system. The birefringent calcite prism allows a user-selectable time delay ($\tau_H - \tau_V$) between horizontal and vertical channels. Interference fringe signals from front and back surfaces of a sample

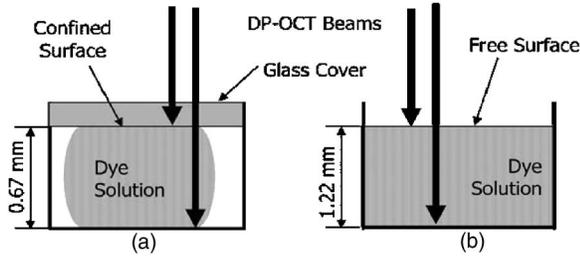


Fig. 2 Sample configuration: (a) Dye solution confined in a glass chamber, and (b) dye solution with one surface exposed to air.

are obtained by adjusting $\tau_H - \tau_V$ introduced by the calcite prism pair.

2.3 Sample Preparation

A 25- μM dye solution (Brilliant Blue, Sigma-Aldrich Company, Saint Louis, Missouri) was used as a sample in this study. The dye has peak absorbance at 585-nm wavelength and is placed in a glass container to measure the laser-induced optical path length change between the air-solution and solution-glass interfaces (see Fig. 2). A transparent plastic cover was positioned over the glass container and used to diminish phase variations induced by evaporation of the dye solution. The optical and physical thickness of the dye solution between the air-solution and solution-glass interfaces was 1.61 and 1.22 mm, respectively. The optical thickness of the dye-solution was measured by DPOCT. Because the air-solution interface was free to move, experiments involving this model are referred to as “free surface.”

The optical path length variation due to thermorefractive change (dn/dT) is measured using another model system. For this experiment, the dye solution is placed between two glass surfaces. The top glass surface was loaded with weights to prevent movement resulting from longitudinal thermal expansion of the dye solution. In addition, the dye solution was allowed to expand laterally to minimize longitudinal movement of the top glass surface. Since DPOCT measures longitudinal optical path length change, contributions due to longitudinal thermal expansion of the confined dye solution are eliminated in this model system. The optical and physical thicknesses of the dye solution were 0.88 and 0.67 mm, respectively. Because the glass-solution interfaces were fixed, experiments involving this model are referred to as “confined surface.”

Absorbance of the dye solution was measured by a spectrometer (DU 7400, Beckman, Fullerton, California) with a 1-cm path length sample holder. The absorbance (A) was measured 20 times and found to be 0.7197 ± 0.0016 . The optical absorption coefficient (μ_a) was calculated from the absorbance (A) as

$$\mu_a(585 \text{ nm}) = \frac{2.3026 \cdot A(585 \text{ nm})}{L}, \quad (12)$$

where L is the physical thickness of the dye solution. As a result, the measured absorption coefficient of the dye solution at 585-nm wavelength was $0.1653 \pm 0.0004 \text{ (mm}^{-1}\text{)}$.

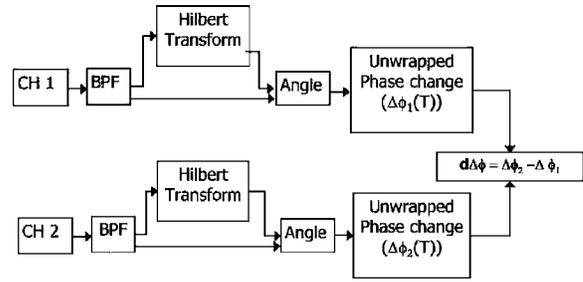


Fig. 3 Signal processing scheme for differential phase calculation.

2.4 Signal Processing for Differential Phase Calculation

A phase-invariant bandpass type 2 Chebyshev filter is used to denoise fringe signals, and a Hilbert transform is used to calculate phase. The phase change is unwrapped to avoid phase jumps, and differential phase ($\Delta\phi = \phi_2 - \phi_1$) is obtained by subtracting two channel phases.¹⁶ Schematic of the signal processing is shown in Fig. 3.

The optical path length change [$\delta(T)$] determined from differential phase change ($d\Delta\phi$) is calculated by:

$$\delta(T) = \frac{\lambda_0}{4\pi} d\Delta\phi, \quad (13)$$

where λ_0 is center wavelength of the DPOCT source.

2.5 Laser Irradiation and Temperature Increase Measurement

A flash-lamp pumped pulsed dye laser (SPTL-1, Candela Corporation, Wayland, Massachusetts) was used to irradiate the dye solution at a range of energies. Determination of temperature increase at the surface of the dye solution is required to compare measured optical path length changes with predicted values using thermophysical properties of water.

For a range of temperature increases, laser irradiance with different laser energies is required. Reflected laser intensity from a cover slip, positioned in the sample arm of the DPOCT system, was detected by a photoreceiver (model 1623, New Focus) during the laser pulse (pulse duration: 400 to 500 μs). Simultaneously, laser energy at the surface of the dye solution was measured by an energy meter (EPM 2000, Moletron, Portland, Oregon).

The laser intensity was integrated with respect to time, and the time-dependent pulsed laser energy with different powers was measured (see Fig. 4). A conversion ratio (κ) from the integrated laser intensity to pulsed laser energy was determined to calculate temperature change in the dye solution [Eq. (14)].

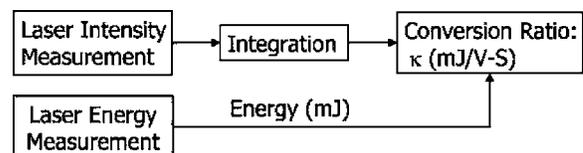


Fig. 4 The schematic of laser-induced surface temperature change measurement.

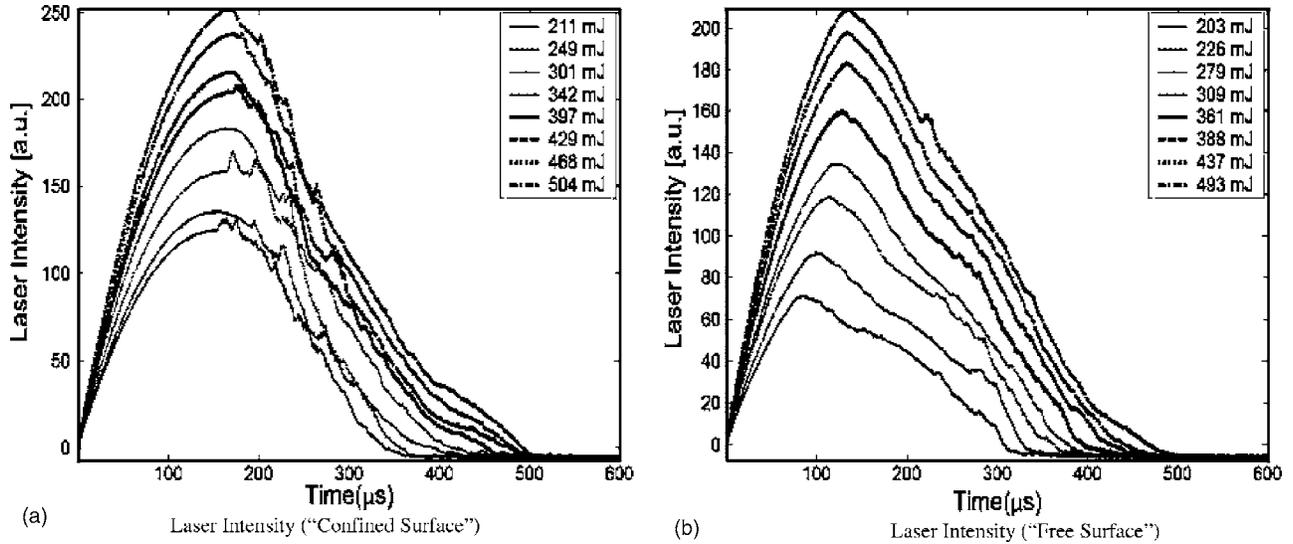


Fig. 5 Detected laser intensity for surface temperature increase measurement. (a) shows measured laser intensities for the confined surface and (b) shows laser intensities for the free surface case.

Furthermore, the mirror reflectivity and angle of incident light on the dye solution were measured. Fresnel reflection (R) from the glass and plastic covers were measured for confined surface and free surface experiments, respectively.

The laser energy irradiating the sample was calculated by the product of the measured laser energy and the net transmission coefficient (T_{net}). The net transmission coefficient of the laser energy is the product of mirror reflectivity (R_{mirror}) and the Fresnel transmission coefficient ($1-R$). The temperature increase (ΔT_0) at the surface of the dye solution was calculated as:

$$\Delta T_0 = \frac{\mu_a \cdot \alpha \cdot \int_0^{\tau} I(t) dt / \text{area}}{\rho \cdot C_p}, \quad (14)$$

where μ_a is the measured absorption coefficient of the dye solution, $\alpha (= \kappa \cdot T_{net})$ is a net conversion ratio that is a product of the conversion ratio (κ) and the net transmission coefficient (T_{net}), “area” is a spot area ($=16.6 \text{ mm}^2$, diameter $\sim 4.5 \text{ mm}$), ρ is density, and C_p is heat capacity at constant pressure.

3 Results

3.1 Laser-Induced Temperature Increase

The measured laser intensities for both confined surface and free surface cases show 400- to 500- μs pulse durations, which is shorter than thermal diffusion time ($=11.5 \text{ s}$) and linear increase with higher laser energy (Fig. 5). The conversion ratio (κ , mJ/V-s) between the intensity integral and laser energy is 8491 [mJ/V-s] Computed net transmission coefficients are:

$$T_{net,confine} = R_{mirror} \cdot (1 - R_{glass}) = 0.684$$

$$T_{net,free} = R_{mirror} \cdot T_{plastic} \cdot (1 - R_{solution}) = 0.66, \quad (15)$$

where $T_{net,confine}$ and $T_{net,free}$ are net transmissions for confined surface and free surface experiments, respectively.

Moreover, $R_{mirror}(=0.74)$ is mirror reflectivity, $R_{glass}(=0.076)$ and $R_{solution}(=0.023)$ are Fresnel reflection coefficients²³ from the glass lid and the dye solution, respectively, and $T_{plastic}(=0.913)$ is measured transmission through the plastic cover. The net transmission is included in the conversion ratio to obtain irradiance at the surface of the dye solution. The net conversion ratio (α) for confined and free surface experiments are 5808 [mJ/V-s] and 5604 [mJ/V-s] , respectively.

3.2 Differential Phase Change

The measured differential phase changes for free surface and confined surface experiments are shown in Fig. 6. For the confined surface experiment, the thermorefractive change governed the measured differential phase change. In the free surface experiment, the thermoelastic and thermorefractive changes contributed to the differential phase change. The corresponding optical path length decreases for the confined surface case, and the optical path length for the free surface case increases in response to laser irradiation.

Larger differential phase changes were detected in response to greater absorbed laser energy in the dye solution. The differential phase decreases for the confined surface case and increases in the free surface case. The differential phase increase due to thermal expansion is stronger (about two times) than that due to water refractive index decrease (Fig. 6).

4 Discussion

The optical path length change due to thermorefractive change and thermoelastic surface displacement of a dye solution in response to pulsed laser heating was investigated by

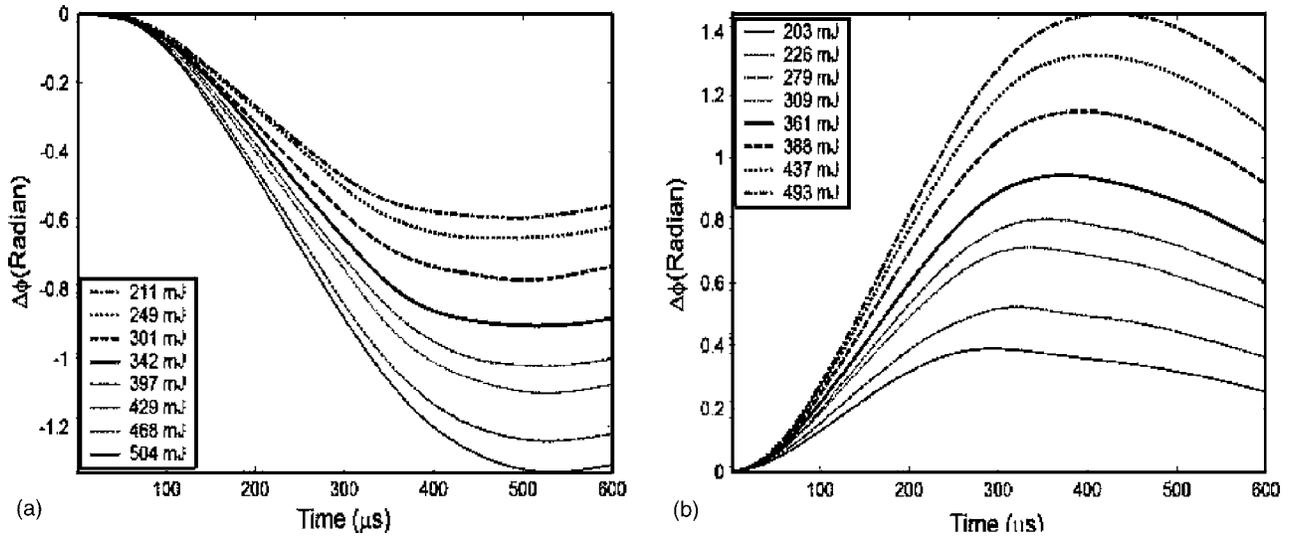


Fig. 6 Differential phase change during a pulse duration for (a) confined surface case and (b) free surface case. Averaged pulsed laser energy is shown in legend.

correlating detected differential phase change ($d\Delta\phi$) and temperature increase (ΔT_0). Values for dn/dT and $n(T_0)\beta(T_0) + dn/dT$, for confined surface and free surface experiments, respectively, were obtained using the curve-fitted linear temperature dependence term (C_1) in Eq. (9).

A linear differential phase decrease observed in the confined surface experiment (Fig. 7) is due to refractive index decrease of water in the dye solution.

The measured dn/dT is $-2.3 \cdot 10^{-4} \pm 7.3 \cdot 10^{-6}$ (1/K). The only available data to validate our result are the temperature-dependent water refractive index estimated by the National Institute of Standards and Technology (NIST) formulation that gives $dn/dT = -9.45 \cdot 10^{-5}$ (1/K) at $1.31 \mu\text{m}$ at constant atmospheric pressure ($=0.1 \text{ MPa}$) from 20 to 30°C . The measured dn/dT is about two times greater than the NIST value. The difference between the values is believed to be due to lateral thermal expansion of the dye solution, which is not

properly accounted for in our 1-D model. The lateral thermal expansion decreased the density and resulted in a lower dn/dT value than that given by NIST data. A constrained surface experiment with a larger spot diameter that better matches the 1-D model will provide a measured dn/dT closer to the NIST value.

The differential phase change in the free surface experiment shows a cubic dependence on temperature increase due to both thermal expansion and refractive index change (Fig. 8). The $n(T_0)\beta(T_0) + dn/dT$ was obtained by a curve fit to differential phase change data. The measured $n(T_0)\beta(T_0) + dn/dT = [1.74 \cdot 10^{-4} \pm 1.7 \cdot 10^{-6}$ (1/K)] closely matches the NIST value $[=1.77 \cdot 10^{-4}$ (1/K)].

We have derived an analytical equation that includes thermoelastic surface displacement and thermorefractive index change that predicts optical path length change in response to pulsed laser irradiation for both confined and free surface

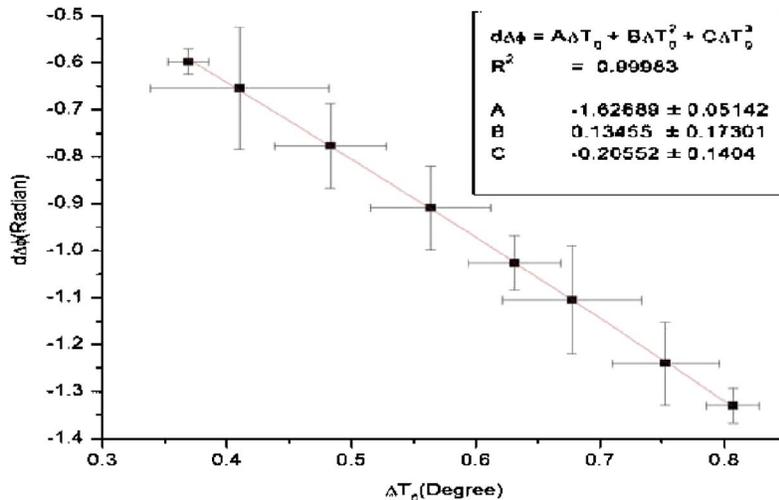


Fig. 7 Differential phase change due to temperature increase in the confined surface case.

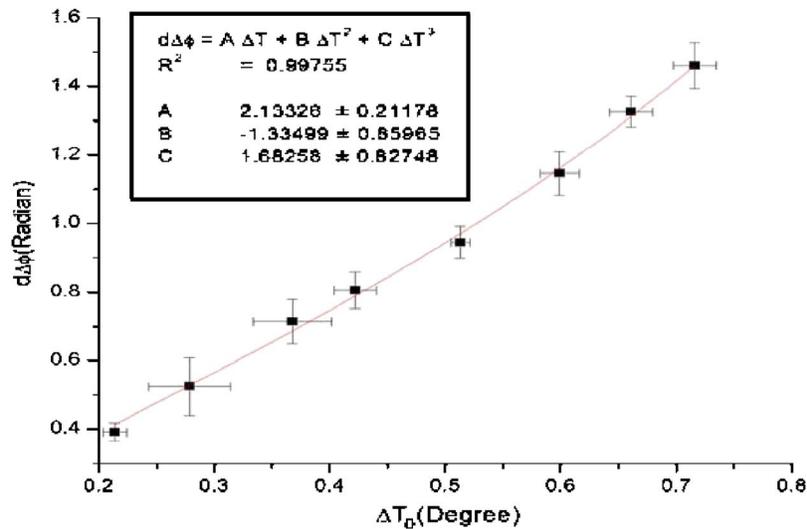


Fig. 8 Differential phase change due to temperature increase in the free surface case.

model systems. Validity of the derived equation was tested by completing experiments using free and confined surface model systems. Results of the experiments allowed us to deduce values for the thermorefractive index change and thermal expansion coefficient at $1.31 \mu\text{m}$ with comparison to published data (NIST). The difference in measured value of dn/dT with that given by NIST may be due to lateral thermal expansion of the heated dye solution that is not accounted for in the 1-D model. A higher power laser that gives a larger spot size is necessary to test DPOCT data within the context of the 1-D model presented here. Since DPOCT can detect dynamic optical path length change in response to pulsed laser irradiation with high sensitivity, applications to tissue diagnostics may be possible.

Quantitative interpretation of optical path length changes in tissue in response to pulsed laser irradiation, however, will require knowledge of changes resulting from thermoelastic and thermorefractive changes of specific tissue constituents. Because tissues consist principally of water and proteins, results reported here are expected to have value in understanding the response of protein-water composite systems such as tissue. The application of DPOCT to tissues will require additional studies that investigate the thermoelastic and thermorefractive responses of proteins. In addition, effect of water-protein interfaces on the thermoelastic and thermorefractive response will require further study for quantitative application of DPOCT to tissues. Experiments to investigate the thermoelastic and thermorefractive response of protein-water systems are underway in our laboratory and will be reported in the future.

Acknowledgments

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