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Abstract. We show that phase-conjugation by three-wave mixing allows turbidity suppression through biological tissues with thicknesses up to 5 mm, at a near-infrared wavelength included in the therapeutic window. Because of the ultrafast character of the imaging process, a motion of the tissue, which mimics *in vivo* imaging, can be exploited to significantly improve the signal-to-noise ratio and the resolution of the restored images. © 2013 Society of Photo-Optical Instrumentation Engineers (SPIE) [DOI: [10.1117/1.JBO.18.11.111405](https://doi.org/10.1117/1.JBO.18.11.111405)]

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1 Introduction

Biological media scatter and diffuse light with negligible absorption at red and near-infrared wavelengths in the optical therapeutic window. Until the 1990s, optical imaging in these media was performed with two distinct groups of methods. First, coherent methods, like optical coherence tomography,¹ used ballistic light, i.e., light scattered one time at most. These coherent methods are limited to depths smaller than 2 mm, because for greater depths all light is multiply scattered and no interferometric signal remains for image reconstruction. Second, for thicker tissues, various incoherent methods were developed that use the scattered light, like diffuse imaging, i.e., reconstruction by computation from diffused waves (Ref. 2 and references therein), time gating to isolate the less diffused photons,³ acousto-optic methods,^{4,5,6} and imaging by two-photon absorption.⁷

In recent years, this distinction has vanished by considering scattering in a static medium as a deterministic phenomenon that can be reversed. It was demonstrated 40 years ago⁸ that a wave scattered by a ground glass slide can be recovered and restored to its initial state by applying optical phase-conjugation and back-propagation through the same slide. A recent experiment by Yaqoob et al. showed that such a scheme can also be applied to a biological medium,⁹ though not *in vivo*. An image transmitted through chicken breast was recorded as a hologram in a photorefractive crystal, which was then restored by back-propagation of the phase-conjugated (PC) wave through the same biological medium. Since the position of the scatterers did not change between forward and backward propagation, the image resolution was preserved. Because of the strong absorption of the 532-nm wavelength used in the experiments, the thickness was limited to 0.7 mm, and the acquisition time in the minute range did not allow studying *in vivo* biological media, which typically have a decorrelation time of 0.1 ms.¹⁰ In later experiments, a collimated beam (no image) was

reconstructed either through 7 mm of the thickness of a chicken breast¹¹ or the ear of a living rabbit.¹² More recent works proposed schemes of time reversal of ultrasound-encoded light, which combine optical phase-conjugation with ultrasound encoding. In such devices, the phase-conjugation process is ensured either by a spatial light modulator¹³ or by a gain medium.¹⁴

Several years ago, we showed that nonlinear $\chi^{(2)}$ imaging by three-wave mixing (i.e., optical parametric amplification of images) allows instantaneous phase-conjugation of a near-infrared (IR) image and its restoration when the image is distorted by an aberrant plate.¹⁵ This method is one of the numerous methods that allows the ultrafast suppression of image distortions by phase-conjugation, for example, through a clear plastic using a hybrid amorphous silicon/ferroelectric-liquid-crystal device,¹⁶ through turbulent atmosphere using sodium vapor¹⁷ or through textured plastic sheets using stimulated Brillouin scattering.¹⁸ In all these experiments, the distorting medium was transparent, and our own experiments with such a type of medium (aberrant glass plate) showed that depolarization of light is negligible even in situations where direct imaging is impossible.

In this paper, we make use of three-wave mixing phase-conjugation (TWMP) to recover IR images transmitted through biological tissues with thicknesses up to 5 mm. We propose to take advantage of a motion of the diffusing medium to significantly improve the signal-to-noise ratio (SNR) and the resolution of the restored images, because of the almost instantaneous character of the nonlinear process. Moreover, we show that the strong depolarization of light due to the scattering process does not prevent image restoration.

2 Experimental Results

2.1 Principle and Experimental Setup

The experimental setup is depicted in Fig. 1. The signal pulses at $\lambda_s = 1.064 \mu\text{m}$ are delivered by a partially frequency-doubled Q-switched mode-locked Nd:YAG laser (PL2250 Series from

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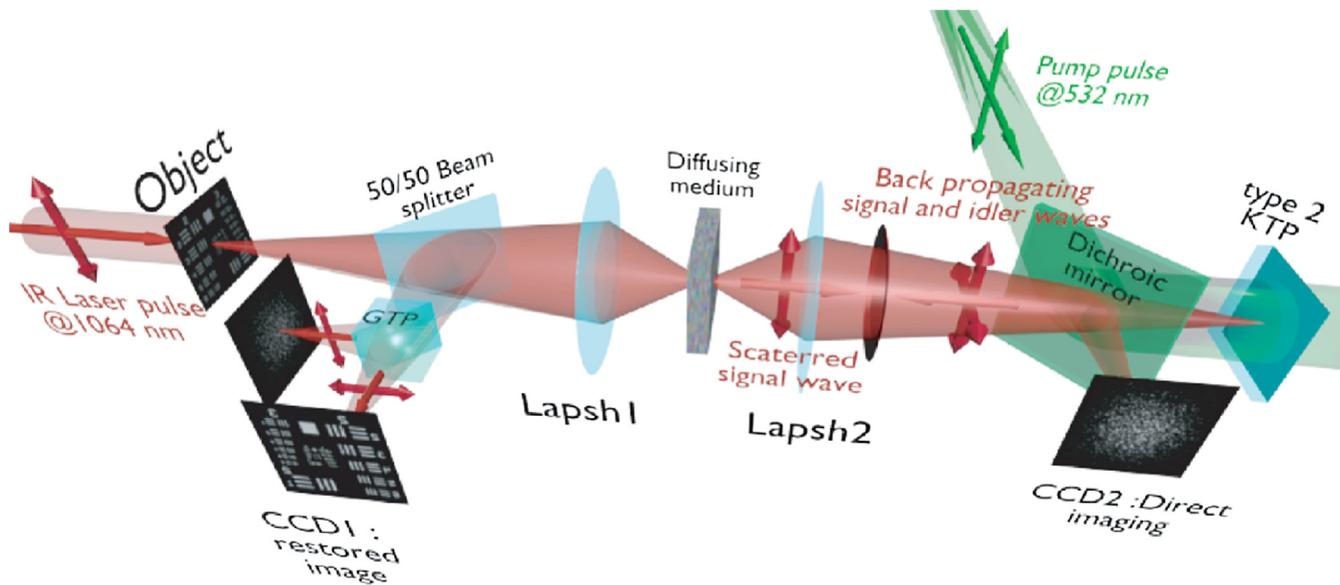


Fig. 1 Experimental setup.

EKSPLA). The nearly TEM₀₀ IR pulses have a 20-ps duration (FWHM), a time-bandwidth product close to 1, and a 10-Hz repetition rate. The pump pulses at $\lambda_p = \lambda_s/2 = 0.532 \mu\text{m}$ are provided by partial frequency-doubling of the IR radiation in a potassium dihydrogen phosphate crystal. The remaining IR light is separated from the green light by a dichroic mirror and then attenuated and vertically polarized. The IR pulses illuminate a resolution target, whose image is formed inside the diffusing medium (biological tissues or translucent adhesive ribbon) with a magnification of 1/20 by means of an aspherical lens with a focal lens of 8 mm and a numerical aperture of 0.5. During the imaging process, the diffusing medium can be moved either in the transverse plane or along the propagation axis. The output scattered light is then collected with a second identical aspherical lens that conjugates the image plane of the first lens with the input face of the nonlinear crystal. The total magnification of the imaging system between the object and the crystal is close to 1. The $5 \times 5 \text{ mm}^2$ wide and 2.5 mm long potassium titanyl phosphate (KTP) crystal from Cristal Laser SA is cut for degenerate type 2 collinear phase-matching¹⁹ and its 20 mrad phase-matching angular range is adapted to the numerical aperture of the imaging system. The neutral axes of the crystal are oriented respectively along the vertical and the horizontal directions. The pump pulse reflected by a dichroic mirror is mixed with the IR scattered signal wave in the KTP crystal. A small amount of the scattered light reflected by the dichroic mirror is used to directly observe the light transmitted through the diffusing medium. Direct imaging through the diffusing medium is performed with a charge-coupled device (CCD) camera (CCD2) placed in the image plane of the second aspherical lens.

In a degenerate three-wave mixing interaction, the idler wave is generated at the same wavelength as the signal and with a transverse wave-vector opposite to that of the signal [Fig. 2(a)], giving forward phase-conjugation¹⁹ [Fig. 2(b)]. In this work, as in Ref. 15, the idler wave is back-reflected by the coated exit face of the crystal (high reflecting coating at $1.064 \mu\text{m}$), resulting in reversing the longitudinal component of the idler wave vector that leads to full phase-conjugation [Fig. 2(c)]. The reflected waves (amplified signal and idler) back-propagate toward the diffusing medium. The PC image is formed by

the idler wave at a symmetric position of the object with respect to the 50/50 beam-splitter and recorded on a low-noise CCD camera (CCD1: Princeton Instruments, Spec-10 400B). A Glan-Taylor polarizer placed in front of CCD1 rejects the vertically polarized distorted signal wave and transmits the horizontally polarized idler wave carrying the PC image. We assume here that the PC image keeps its horizontal polarization while back-propagating in the diffusing medium. This nontrivial issue will be discussed in the next section. The signal amplification gain G_s , defined as the ratio between the signal pulse energies with and without amplification, has been measured, giving a value close to 2. Because the added power on the signal is, for identical signal-idler wavelengths, equal to the generated idler energy, the gain of phase conjugation G_{PC} , defined as the ratio between the incident signal energy and the energy of the PC wave, is given by $G_{PC} = (G_s - 1)$.

2.2 Diffusing Media

In these experiments, two kinds of diffusing media are studied. The first one consists of a translucent adhesive ribbon fixed on a 1-mm-thick microscope slide. The value of the ribbon thickness is a few tens of microns and the light traversing the rough surface evolves in a fully developed speckle. From measurements of the size of the speckle halo, the mean size of the diffusing grains is estimated to be $1 \mu\text{m}$. The degree of polarization of the scattered light is given by the ratio I_{\parallel}/I_{\perp} , where I_{\parallel} and I_{\perp} are, respectively, the energies of the scattered light, measured in the parallel and orthogonal polarization directions with respect to the polarization direction of the incident light. A ratio of 385 ± 35 is measured while this ratio is 500 through the clean microscope slide. Thirty-five percent of loss due to scattering is also measured by comparing the energies transmitted through the imaging system with and without the diffusing medium. These results indicate that, with this kind of medium, most of the light is scattered in the forward direction and the scattering process is almost polarization independent. With such a thin scattering medium, direct imaging is possible with a good SNR when the object is imaged at the surface of the diffusing medium [Fig. 3(b)], because of the so-called shower

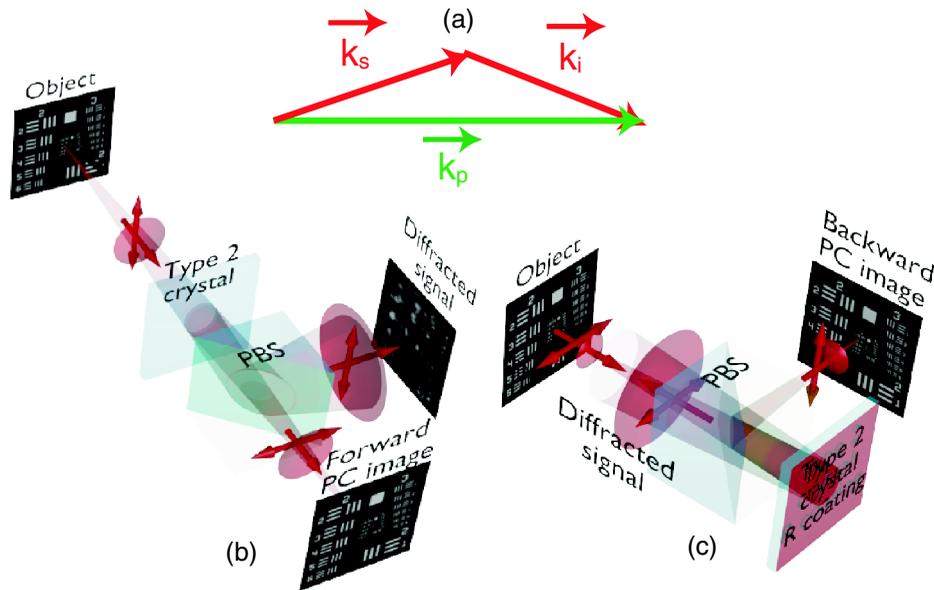


Fig. 2 (a) k-wavevector diagram for noncollinear three-wave mixing. (b) Principle of forward three-wave mixing phase-conjugation imaging. (c) Full phase-conjugation by three-wave mixing. The horizontal and vertical arrows represent the crossed polarization directions of the signal and idler waves in a type 2 interaction. For the sake of clarity, the pump plane wave is not represented.

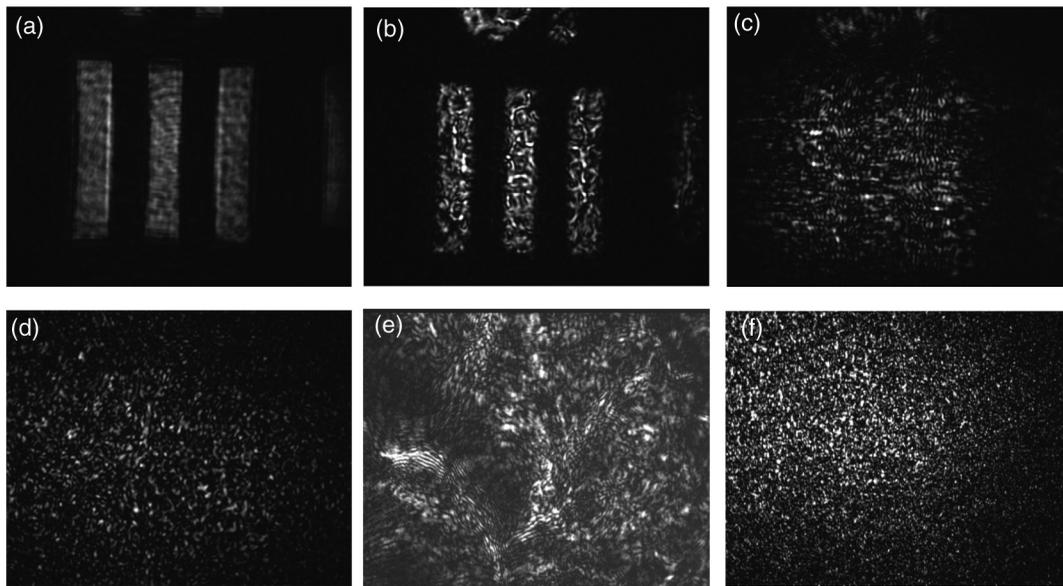


Fig. 3 Results of direct imaging results through different media: (a) The clean microscope slide. (b) and (c) One layer of translucent adhesive ribbon when the image of the object is formed on the diffusing medium and when the diffusing medium is placed before the image plane, respectively. (d) Two layers of adhesive ribbon on both faces of the microscope slide. (e) and (f) Biological tissues: 0.7-mm-thick Parma ham slice and 5-mm-thick chicken breast, respectively.

curtain effect.²⁰ An SNR close to 2 is deduced from the peak value of the normalized covariance function cov_{\max} (Ref. 21) between the image obtained through the clean microscope slide [Fig. 3(a)] and the image obtained through the diffusing medium [Fig. 3(b)], such that

$$\text{SNR} = \frac{\text{cov}_{\max}}{1 - \text{cov}_{\max}}. \quad (1)$$

In the direct imaging configuration, the image resolution is limited by the size of the speckle grains. When the diffusing medium is placed before or after the image plane, the image of the object is completely blurred and the object can no more

be recognized [Fig. 3(c)]. For the sake of comparison, a second layer of adhesive ribbon was fixed on the other face of the microscope slide. In this case, direct imaging is impossible even when the object is imaged on the first adhesive ribbon layer [Fig. 3(d)] and whatever be the position of the image plane with respect to the diffusing medium.

The second kind of diffusing media that we studied consists of two different biological tissues. The first one is formed with slices of Parma ham with thicknesses from 0.7 to 2.1 mm and the second one is a 5-mm-thick piece of chicken breast. The tissues are maintained between two microscope slides. With a standard scattering coefficient $\mu_s = 100 \text{ cm}^{-1}$ and an anisotropy

coefficient $g = 0.9$, the reduced scattering coefficient is $\mu'_s = \mu_s(1 - g) = 10 \text{ cm}^{-1}$. Then, the thicknesses of the biological samples, expressed in number of reduced scattering mean free paths (mfp_l), lie in the range 0.7 to 5 mfp_l . We measured the degree of polarization and losses through the two kinds of biological tissues for the translucent adhesive ribbon as well. Average degrees of polarization of 20, 10, and 2 and losses of 50, 90, and 97% have been measured, respectively, for 0.7- and 2.1-mm-thick slices of Parma ham and a 5-mm-thick piece of chicken breast. It should be stressed that the studied biological tissues (consisting of muscle fibers and fats) are very inhomogeneous. Therefore, these measurements fluctuate with large amplitudes depending on the area crossed by the light. Finally, we verified that direct imaging is impossible through biological tissues [Fig. 3(e) and 3(f)], whatever be the position of the diffusing medium with respect to the intermediate image plane.

2.3 Image Restoration by Three-Wave Mixing Phase-Conjugation

In this section, we present the results of image restoration by backward propagation of the PC idler wave through diffusing media. We have investigated the resolution limits in restored images as well as the consequences of a motion of the diffusing medium during the acquisition time. Figure 4(a) shows the limits of resolution in images formed by the backward PC wave propagating through the clean microscope slide. In this image, the line group 16 mm^{-1} of the USAF resolution chart is resolved. Since the magnification of the imaging system between the object and the type 2 KTP crystal is close to 1, it corresponds also to a resolution of 16 mm^{-1} in the crystal, which is in good agreement with the theoretical resolution given by the phase-matching conditions.²² Figure 4(b) shows the PC image obtained through one static layer of translucent adhesive ribbon positioned such that direct imaging is impossible. In the restored image, the resolution and the SNR are seriously degraded by the speckle noise. The 5.04 mm^{-1} line group

can be recognized and an SNR equal to 2 is measured. As with a static diffusing medium, the speckle noise patterns are strongly correlated from one laser shot to another, and the SNR in PC images can be seriously improved if the diffusing medium moves during the acquisition time. Indeed, in this case, uncorrelated speckle noise patterns are summed by CCD1 during the acquisition time. This speckle averaging reduces the noise fluctuations and therefore improves the SNR of the PC images. In these experiments the acquisition time is 1 s, corresponding to the acquisition of 10 laser shots. Figure 4(c) and 4(d) clearly shows the SNR and resolution improvement when the diffusing medium is moving. These figures correspond to the PC images obtained when, respectively, the medium is moved along the transversal axis (Y) and along the propagation axis (Z). In both cases, the diffusing medium is translated with an amplitude of $\pm 50 \mu\text{m}$ around its initial position during the exposure time of CCD1. In PC images, the 16 mm^{-1} line group of the USAF resolution chart is now resolved and an SNR equal to 4 is deduced from the normalized covariance function [Fig. 4(e)] calculated between Fig. 4(a) and 4(d).

The same experiments were performed with a 0.7-mm-thick biological tissue. Figure 5 shows these results with a static medium and a medium in motion. Although the biological tissue is much thicker than the translucent adhesive ribbon, similar performances are obtained: the 14.24 mm^{-1} line group is resolved and an SNR equal to 2.6 is measured. We would like to stress that in the intermediate image plane, the resolution is 285 mm^{-1} according to the $1/20$ magnification of the first aspherical lens. Moreover, surprisingly, we observed that the restored image is linearly polarized in a crossed polarization direction with respect to the incident signal polarization direction. It shows that the process of image restoration by TWMPCC does not require that the back-propagating PC wave has the same polarization state as the scattered signal wave emerging from the scattering medium. This particular point will be discussed in Sec. 3.

The last experiment consists of image restoration through biological tissues with different thicknesses. Parma ham slices of thicknesses 0.7, 1.4, and 2.1 mm and a 5-mm-thick piece of

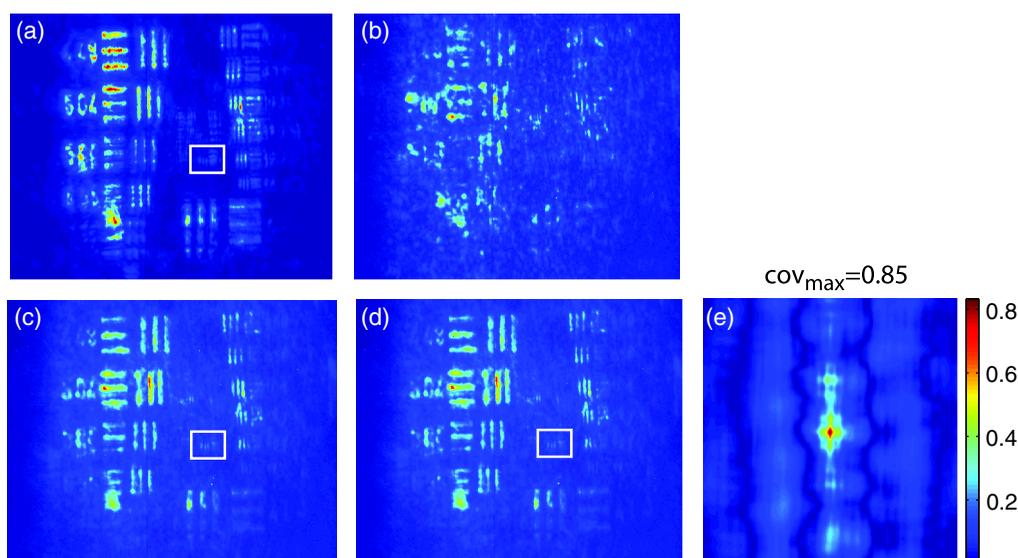


Fig. 4 Resolution limits through translucent adhesive ribbon. (a) Phase-conjugated (PC) image through the clean microscope slide. (b) PC image through a static single layer of translucent adhesive ribbon. PC images when the diffusing medium is moved (c) along the transversal axis (Y) and (d) along the propagation axis (Z) during the acquisition time. White rectangles surround the 16 mm^{-1} line group. (e) Normalized covariance between PC images (a) and (d).

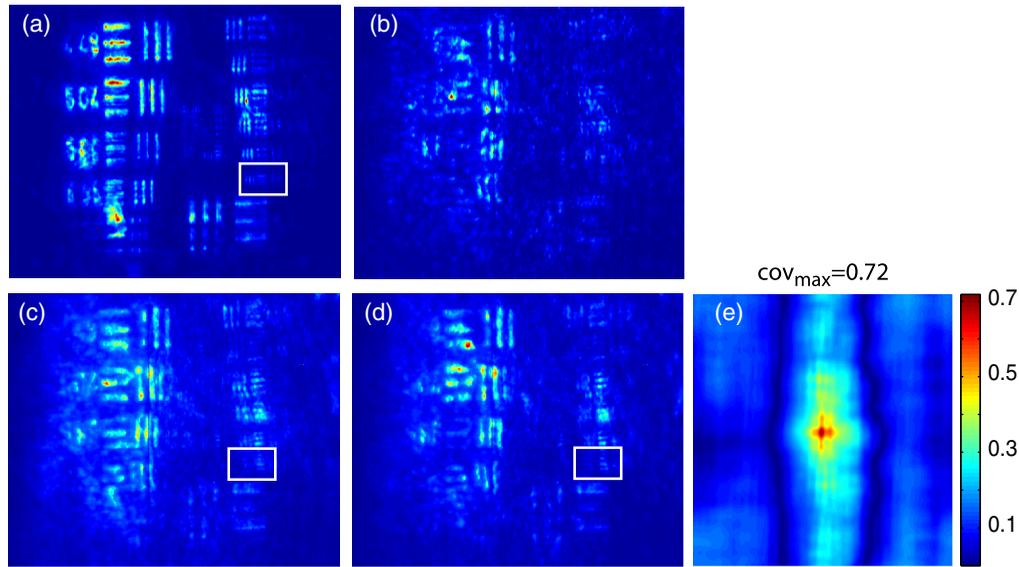


Fig. 5 Resolution limits through 0.7-mm-thick Parma ham slice: (a) PC image through the clean microscope slide. (b) PC image through static biological tissue. PC images when biological tissue is moved (c) along the transversal axis (Y) and (d) along the propagation axis (Z) during the acquisition time. White rectangles surround the 14.24 mm^{-1} line group. (e) Normalized covariance between PC images (a) and (d).

chicken breast were used. Figure 6 shows the PC images of the 1.41 and 2.83 mm^{-1} line groups of the USAF target obtained through the Parma ham and chicken breast samples, respectively. Figure 6(a) and 6(b) corresponds to the PC images of the two line groups obtained through the clean microscope slide. Figure 6(c) to 6(f) corresponds to the PC images obtained through static biological tissues with increasing thicknesses.

Because the PC images are seriously degraded by the speckle noise, the initial object is more and more difficult to recognize when the thickness of the biological tissue increases. When biological tissues are moved during the acquisition time of CCD1, the SNR of PC images is improved significantly as in previous experiments [Fig. 6(g) to 6(j)]. While motion of biological media seriously improves the resolution of PC images, the

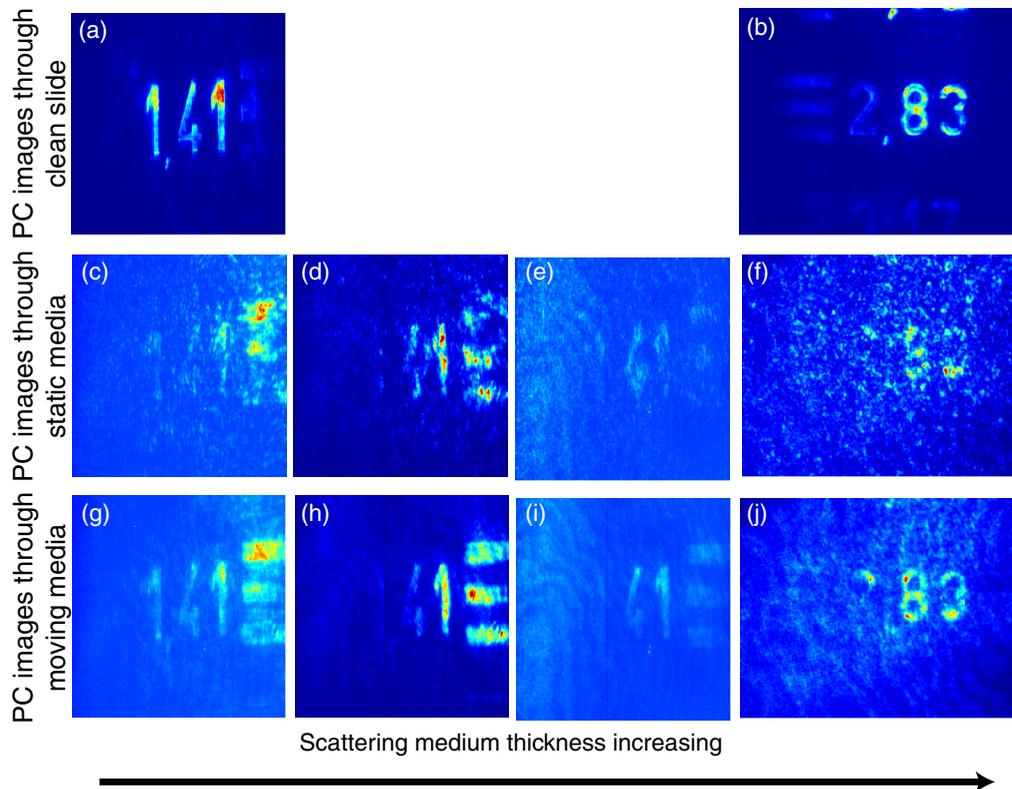


Fig. 6 Image restoration through 0.7- to 5-mm-thick biological tissues. (a) and (b) reference PC images of 1.41 and 2.83 mm^{-1} line groups of the USAF target obtained through the clean microscope slide. (c) to (f) PC images obtained through static biological media with 0.7-, 1.4-, and 2.1-mm-thick Parma ham slices, respectively, and 5-mm-thick piece of chicken breast. (g) to (j) PC images obtained through the same biological tissues moving along Y axis.

SNR clearly decreases when the thickness of the biological tissues increases. Indeed, losses also increase with the thickness. Thus, the PC image is progressively drowned in the background noise, mainly because of the back-scattered light. Experimentally, increased losses are compensated partially by increasing the amplification gain of the nonlinear TWM process (i.e., by increasing the pump pulse energy).

3 Discussion

In Sec. 2.2 we report measurements of the degree of polarization of the scattered light by different media. We show that, unlike for a thin diffusing medium, the light transmitted through biological tissues is strongly depolarized. As it is explained in Sec. 2.1, in a type 2 TWM interaction, the signal wave is usually polarized along one neutral axis of the nonlinear birefringent crystal (for example, the ordinary polarization direction). Because of the type 2 phase-matching conditions, the generated idler wave is polarized in the crossed direction (i.e., the extraordinary polarization direction). Then in our experiment a Glan-Taylor polarizer placed in front of CCD1 allows detection of the idler wave carrying PC images and rejects the signal wave. When the scattering process is more or less polarization independent, like through a translucent adhesive ribbon, image restoration can be obtained with a PC wave having a polarization direction different from that of scattered light. Through biological tissues where light is strongly depolarized, we clearly observed that restored images carried by the PC idler wave are linearly polarized in a perpendicular direction with respect to the polarization direction of the incident signal light.

This surprising result can be explained using the scattering model of a plane wave light by a dielectric sphere.²³ In our

model, we have chosen dielectric spheres in water with a refractive index of 1.588 at 1.064 μm and a diameter of 1.4 μm , such that the anisotropy coefficient g given by the Mie theory²³ is equal to 0.91. With this model, $(\vec{E}_{sc}^{\parallel}, \vec{E}_{sc}^{\perp})$, the electric field components of the scattered light expressed in the parallel and perpendicular directions of the scattering plane can be calculated for every scattering direction. The scattering directions are characterized by the usual polar angles (θ, ϕ) , where the angle θ is randomly calculated with a probability distribution deduced from the Henyey-Greenstein phase function²⁴ and the angle ϕ is randomly selected in the range $[0, 2\pi]$ rad with a uniform probability distribution. Only the output scattered fields with propagation directions included in the numerical aperture of 0.5 of our imaging system, which is limited by the phase-matching angular acceptance of the nonlinear crystal, are phase-conjugated. The proportion of realizations that do not fit this criterion gives approximately the losses due to scattering in our model. Figure 7(a) shows typical scattering paths for a set of 20 realizations when five scattering events are considered.

After one or several scattering events, the output scattered field \vec{E}_{sc} [Fig. 7(a)] is calculated on the (\vec{e}_x, \vec{e}_y) basis (corresponding to the neutral axes of the nonlinear crystal) and is phase-conjugated following the coupled-wave equations of type 2 TWM interaction:

$$\begin{cases} E_{PC_x} \propto -iE_{sc_y}^* \\ E_{PC_y} \propto -iE_{sc_x}^* \end{cases} \quad (2)$$

Then, the scattering process is reversed. In principle, a complete time reversal requires a phase-conjugate mirror (PCM) of constant reflectivity for all input directions and polarizations to

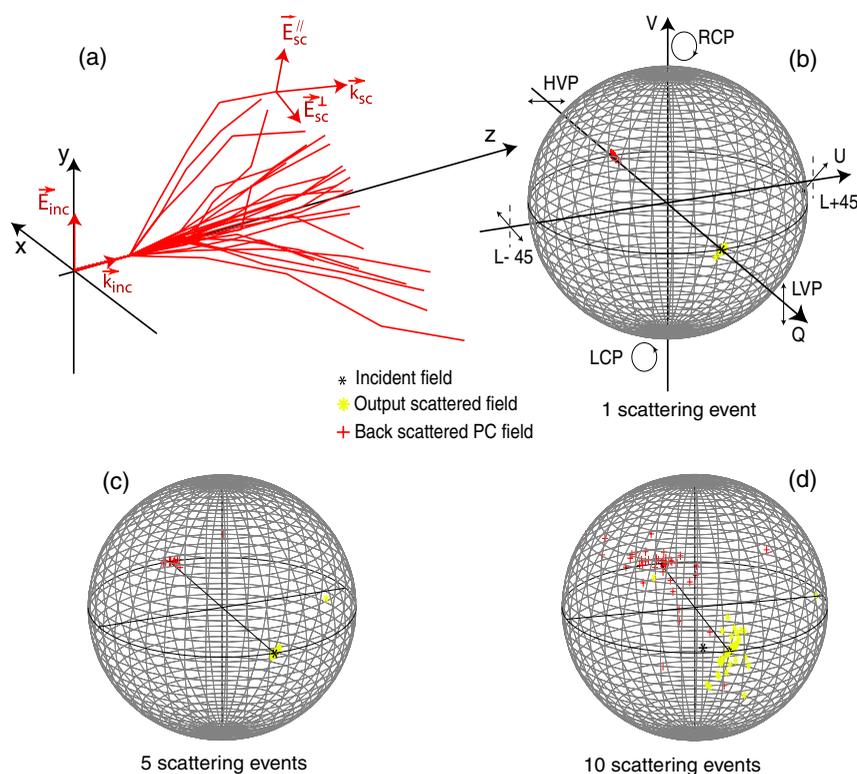


Fig. 7 (a) Typical scattering paths when five scattering events are considered. (b) to (d) Representations of the normalized Stokes parameters $[Q, U, V]$ on the Poincaré sphere of the output scattered fields (yellow stars) and the back-scattered PC fields (red crosses) when 1, 5, or 10 scattering events are considered. The black star denotes the vertical polarization state of the incident light.

Table 1 Losses and mean values of the normalized Stokes parameters $[Q, U, V]$ of the back-scattering phase-conjugated fields for 1, 5, and 10 scattering events. Calculations are made with sets of 500 realizations.

Number of scattering events	Losses in %	Q	U	V
1	10	-1.000 ± 0.001	0.00 ± 0.02	0.00 ± 0.03
5	60	-1.00 ± 0.09	0.0 ± 0.3	0.0 ± 0.2
10	80	-0.9 ± 0.2	0.0 ± 0.4	0.0 ± 0.4

capture the entire scattered wavefront. In practice, such a mirror is difficult to achieve and often only a small portion of the wavefront of a single polarization can be captured and time-reversed like with PCM based on four wave-mixing processes. Therefore, we would like to emphasize that with type 2 TWMP, all polarization directions are phase-conjugated.

The polarization state of light at each step of the process is characterized by its Stokes parameters $[I, Q, U, V]$ that can be positioned on the Poincaré sphere. Figure 7(b) to 7(d) depicts the polarization state of the output scattered fields (yellow stars) and the back-scattered PC fields (red crosses) when 1, 5, or 10 scattering events are considered. The incident light is vertically polarized here. Each yellow star and red cross correspond to one realization. With this model, Fig. 7(b) to 7(d) shows that the polarization directions of the back-propagating PC waves that retrace the scattering path are more or less horizontally polarized, i.e., in a direction perpendicular to the initial polarization direction of the incident light. When the number of scattering events increases, the dispersion of the polarization states of the PC fields around the horizontal polarization direction as well as losses estimated by the proportion of realizations that do not fit the criterion related to the numerical aperture of the imaging system increase. Hence, the realizations that fit this numerical aperture correspond also to nearly horizontally polarized light. Table 1 summarizes the losses and the mean values of the normalized Stokes parameters $[Q, U, V]$ of the back-scattering PC fields calculated for 1, 5, and 10 scattering events with sets of 500 realizations.

Although biological tissues are more complex media than dielectric spheres, this demonstration is consistent with our experimental observations.

4 Conclusion

We have developed an ultrafast method of near-IR imaging through biological tissues by compensation of the turbidity of these media. This method is based on instantaneous phase-conjugation by three-wave mixing in a type 2 nonlinear quadratic crystal. Imaging through biological tissues with thickness up to 5 mm has been performed. Furthermore, we showed that this method works either with static or with moving scattering media, with a significant improvement of SNR and resolution in the latter case. Finally, we have shown that a type 2 TWM process leads to a polarization rotation of the PC wave with respect to the incident wave that does not preclude the image restoration process.

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